

↳ Same # of heads and tails

0 0 0 0 0 0 0 0

$$\binom{8}{4}$$

(22) ABCDEFGH

ED

permutation - cannot repeat letters.

* A, B, C, ED, F, G, H
7!

$$0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \\ 7 \times 6 \times 5 \times \dots \times 1 = 7!$$

↳ BA and FG H?

BA, C, D, E, FG H

0 0 0 0 0

$$5 \times 4 \times 3 \times 2 \times 1 = 0$$

Recitation class

NOV 25, 2014

Q.1 $n=6$

(12) 000000

222222 2^6

$n=5$ 00000 2^5

0000 2^4

000 2^3

00 2^2

0 2^1

$$\sum_{i=1}^6 2^i$$

$$\sum_{i=1}^n 2^i = 2^{n+1} - 2$$

$\hookrightarrow 2^7 - 2 = 126$

But this answer is enough

$$\textcircled{K1} \textcircled{1} \underbrace{00 \dots 00}_{n-2} \textcircled{1} = 2^{n-2}$$

(16)

$$\begin{array}{cccc}
 0 & 0 & 0 & 0 \\
 \times & \underbrace{26 & 26 & 26} \\
 \hline
 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 \hline
 0 & 0 & 0 & 0
 \end{array}$$

$$\left. \begin{array}{l}
 + 4 \times 25^3 \\
 + \binom{4}{2} \times 25^2 \\
 + \binom{4}{3} \times 25
 \end{array} \right\} \text{solution.}$$

↳ si cada que sea solo una x por cada string entonces:

$$\begin{array}{cccc}
 0 & 0 & 0 & 0 \times 25^3 \\
 0 & 0 & 0 & 0 \times 25^3 \\
 0 & 0 & 0 & 0 \times 25^3 \\
 0 & 0 & 0 & 0 \times 25^3 \\
 \hline
 4 \times 25^3 =
 \end{array}$$

(20)

$$\begin{array}{r}
 1000 - 9999 \\
 \hline
 91x?
 \end{array}$$

$$\begin{array}{l}
 1 \times 9 \\
 2 \times 9 \\
 3 \times 9 \\
 \vdots
 \end{array}$$

$$1111 \times 9 = 9999$$

then ->:

$$\begin{array}{r}
 1111 \\
 - 111 \\
 \hline
 \end{array}$$

$$111 \times 9 = 999$$

so exclude
#s that r less
than 111.

↳ how many #s in between
1000 - 9999 are even?

$$9999 - 1000 + 1 = 9000 \therefore 2 = \boxed{4500}$$

↳ how many have distinct digits.

$$P_{99} = P_{25} + P_{55} + P_{008} = 19041$$

$$0000$$

$$9 \times 8 \times 7 \times 6 = 3024$$

↳ how many are not divisible by 3?

$$\underline{3 \times 333 = 999} \uparrow$$

:

then subtract
from total

$$3 \times 3333 = 9999$$

↳ divisible by 5 or 7

$$\begin{array}{r} 1999 \\ 5 \overline{) 9999} \end{array}$$

$$2000$$

$$\begin{array}{r} 200 \\ 5 \overline{) 1000} \end{array}$$

$$A = \{x \mid 1000 \leq x \leq 9999, 5 \mid x\}$$

$$\{ 1999 - 200 + 1 = 1800 : |A|$$

$$\begin{array}{r} 1428 \\ 7 \overline{) 9999} \end{array}$$

$$\begin{array}{r} 142 \\ 7 \overline{) 1000} \end{array}$$

$$1428 - 142 = 1286 = |B|$$

$$B = \{x \mid 1000 \leq x \leq 9999, 7 \mid x\}$$

$$* \text{ Now, } |A \cup B| = |A| + |B| - |A \cap B|$$

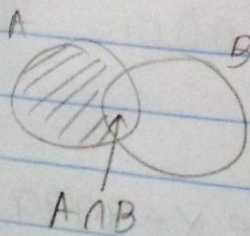
$$|A \cup B| = 1800 + 1286 - 257 = 2829$$

↳ Not divisible by either 5 or 7

$$\overline{A \cup B} = \overline{A \cup B} \rightarrow 9000 - 257$$

↳ Not divisible by 5 but divisible by 7

$$|A \cap \overline{B}| = |A - B|$$



$$|A - |A \cap B| = |A \cap \overline{B}|$$

$$1800 - 257 = 1543$$

6.2³ How many diff. order can we write the governor's names?

-6
-5
-4
-3
-2
-1

O O O O O O
 $6 \times 5 \times 4 \times 3 \times 2 \times 1 = 6!$

6.2

(14) 1-100, choose two pos integers.

1...99

$$99 - 1 + 1 = 99$$

$$\binom{99}{2}$$

(18) coin exercise.

O O O O O O O O

$$2 \times 2 \times 2 \times 2 \times 2 \dots \times 2 = 2^8$$

H T H T H T ... T

↳ exactly four heads and rest tails

$$\binom{8}{2} = \frac{8!}{6!2!} = \frac{8 \times 7}{2} = 28$$

$$28 - 37 = 256 - 37 = 219$$

6.4

$$\textcircled{8} (3x + 2y)^{17} \quad \text{---} \quad x^8 y^9$$

$$(115) \quad (3x + 2y)^n = \binom{n}{0} f^0 s^n + \binom{n}{1} f^1 s^{n-1} + \binom{n}{2} f^2 s^{n-2} + \dots + \binom{n}{n-1} f^{n-1} s^1 + \binom{n}{n} f^n s^0$$

answer: $\binom{17}{8} (3x)^8 (2y)^9$

can
put
8 or 9

$$\binom{17}{8} 3^8 2^9 x^8 y^9$$

coefficient

→ podemos dejarlo expandido.

6.4 prove this

$$\textcircled{22} \binom{n}{r} \binom{r}{k} = \binom{n}{k} \binom{n-k}{r-k}$$

$$\left(\frac{n!}{r!(n-r)!} \right) \left(\frac{r!}{k!(r-k)!} \right) = \left(\frac{n!}{k!(n-k)!} \right) \left(\frac{(n-k)!}{(r-k)!} \right)$$

$$\frac{n!}{(n-r)! \cdot k! \cdot (r-k)!} = \frac{n!}{(n-r)! \cdot k! \cdot (r-k)!}$$

Another exercise

→ of 1st exam.

$$f: A \rightarrow B$$

$$S, T \subseteq A$$

$$\therefore f(S \cap T) \subseteq f(S) \cap f(T)$$

↑
intersection

$$x \in f(S \cap T) \rightarrow x \in f(S) \cap x \in f(T)$$

$$\hookrightarrow x \in f(S) \cap f(T)$$

$$y \in f(S \cap T) \rightarrow \exists x \in S \cap T, f(x) = y$$

$$x \in S \cap T \rightarrow x \in S \wedge x \in T$$

$$\left. \begin{array}{l} x \in S \rightarrow f(x) \in f(S) \\ x \in T \rightarrow f(x) \in f(T) \end{array} \right\} \rightarrow f(x) \in f(S) \cap f(T)$$

$$\rightarrow y \in f(S) \cap f(T)$$

$$\therefore f(S \cap T) \subseteq f(S) \cap f(T)$$